

Technical guide No. 7 - Basic formulas 基本公式

Road show 3
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Technical guide No. 7 - Basic formulas

Purpose and targets of the presentation

内容和目的

- ➡ **Purpose of the presentation 内容**
 - **Show the typical formulas used in basic dimensioning**
说明基本选型公式

- ➡ **The targets of the presentation are that you: 目的**
 - **Can do also manual calculations of basic dynamical systems (e.g. acceleration time)**
动态系统的手工计算

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AC motor - Power 交流电机的功率

- ➔ Motor's mechanical output power can be calculated from speed and torque:

通过速度和力矩计算电机的输出功率

$$P_{out}[kW] = \frac{T[Nm] * n[rpm]}{9550}$$

$$P_{out}[W] = T[Nm] * \omega[rad / s]$$

$$\omega[rad / s] = \frac{2\pi}{60} * n[rpm]$$

$$1 kW = 1000 W$$

- ➔ Motor's input power can be calculated from voltage, current and power factor:

通过电压，电流和功率因数计算电机输入功率

$$P_{in}[W] = \sqrt{3} * U[V] * I[A] * \cos(\varphi)$$

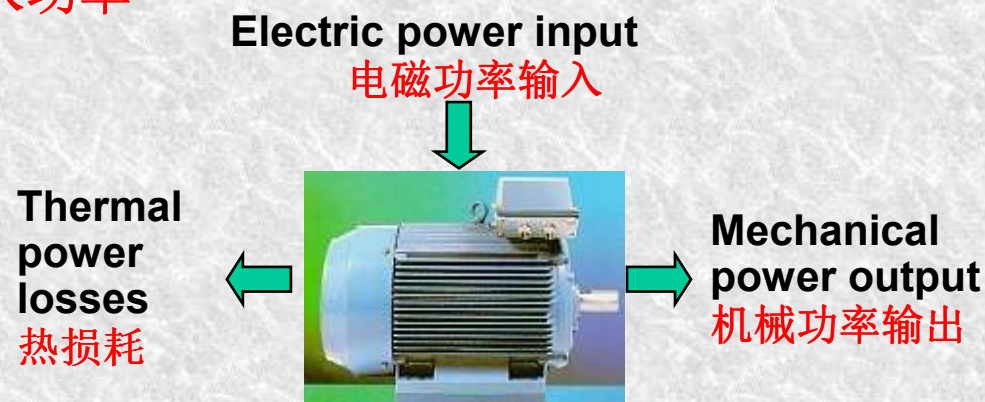
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AC motor - Power 交流电机的功率

- ➔ Motor's efficiency is output power divided by input power:

电机效率是输出功率/输入功率

$$\eta = \frac{P_{out}}{P_{in}}$$



- ➔ At nominal point AC motor's output power is:

电机额定点的输出功率

轴头电功率 $P_{out}[W] = P_n[W] = \sqrt{3} * U_n[V] * I_n[A] * \cos(\varphi_n) * \eta_n$ or

轴头机械功率 $P_{out}[kW] = P_n[kW] = \frac{T_n[Nm] * n_n[rpm]}{9550}$

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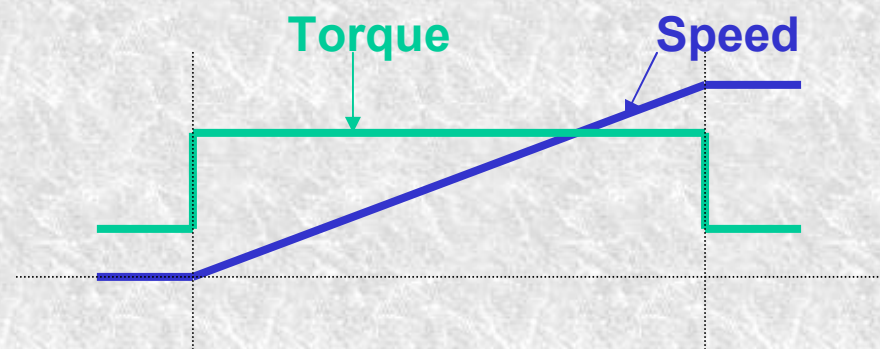
AC motor - Mechanical laws of rotational motion

AC 电机的转动原理

- ➔ One of the fundamental equations for an electric motor is:

电机转子的加速规律

$$J \frac{d\omega}{dt} = T - T_{load}$$



- ➔ Motor torque consists of dynamic and load component. Dynamic component changes the speed:

电机力矩包含动态力矩分量和负载力矩分量

$$T = T_{dyn} + T_{load}$$

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AC motor - Mechanical laws of rotational motion

AC 电机的转动原理

- ➔ Dynamic torque component changes the motor speed:

动态力矩分量影响电机转速

$$T_{dyn}[Nm] = J[kgm^2] * \frac{d\omega[rad / s]}{dt}$$

- ➔ In practice the dynamic component is calculated as follows:

动态分量的工程计算

$$T_{dyn}[Nm] = J[kgm^2] * \frac{2\pi}{60} * \frac{\Delta n[rpm]}{\Delta t[s]}$$

- ➔ The total torque needed in acceleration is thus:

加速过程中总的力矩是

$$T[Nm] = T_{dyn} + T_{load} = J[kgm^2] * \frac{2\pi}{60} * \frac{\Delta n[rpm]}{\Delta t[s]} + T_{load}$$

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AC motor - Mechanical laws of rotational motion

AC 电机的转动原理

Example: AC motor's and load's total moment of inertia is 3 kgm².
Constant load torque is 50 Nm.

举例：电机和负载的总转动惯量是**3 kgm²**，恒定负载力矩**50 Nm**

A) What is the torque needed to accelerate the motor from 0 rpm to 1000 rpm speed in 10 seconds?

问题**A)**：电机转速在**10秒**内从**0**加速到**1000rpm**，需要多大力矩？

B) If the electric supply is switched off at 1000 rpm speed how fast will the motor decelerate to 0 rpm speed?

问题**B)**：如果电机运行在**1000rpm**时，停止供电，
那么电机减速至**0rpm**要多少时间？

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AC motor - Mechanical laws of rotational motion

AC 电机的转动原理

Solution: 答案

A) The total torque needed for acceleration is the sum of dynamic and load components. 加速过程中总力矩是动态和负载力矩之和

$$T = T_{dyn} + T_{load} = 3 * \frac{2\pi}{60} * \frac{1000}{10} \text{ Nm} + 50 \text{ Nm} = 81.4 \text{ Nm}$$

B) The motor decelerates because of the load torque (50 Nm), Actual motor torque is zero. Then:

减速过程中，仅靠负载力矩起作用(50 Nm)，电机本身没有任何力矩起作用

$$J[\text{kgm}^2] * \frac{2\pi}{60} * \frac{\Delta n[\text{rpm}]}{\Delta t[\text{s}]} = -T_{load} \Leftrightarrow \Delta t[\text{s}] = 3 * \frac{2\pi}{60} * \frac{1000}{50} \text{ s} = 6.28 \text{ s}$$

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Moment of inertia & gears 惯性矩和齿轮箱的因素

- 'Inertia' (moment of inertia) is important to know in many dimensioning cases.
选型时必须知道惯性(转动惯量)。
- Generally $J[\text{kgm}^2]$ can be given by motor and machine manufacturers.
制造厂通常给出转动惯量: $J[\text{kgm}^2]$
- Sometimes it can be calculated quite easily. For a cylinder shape the moment of inertia is proportional to mass and quadratically proportional to radius of the cylinder: $J = m \cdot r^2$.
转动惯量很容易计算。
圆筒型的转动惯量与其质量和半径的平方成正比: $J = m \cdot r^2$
- Energy stored to a rotating mass is: $E = 0.5 \cdot J \cdot \omega^2$
旋转体储存的能量是: $E = 0.5 \cdot J \cdot \omega^2$

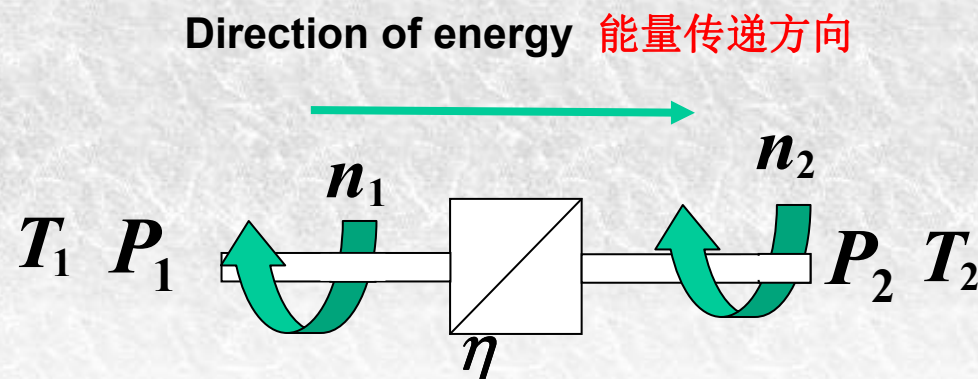
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Moment of inertia & gears 惯性矩和齿轮箱的因素

- ➔ When gear is used power, torque, moment of inertia, spring constant of a shaft, etc. must be reduced.

使用齿轮箱时，功率，转矩，转动惯量，轴的弹性系数等必定会减小

$$T_1 = \frac{T_2}{\eta} * \left(\frac{n_2}{n_1} \right)^2 \quad J_1 = J_2 * \left(\frac{n_2}{n_1} \right)^2 \quad P_1 = \frac{P_2}{\eta}$$

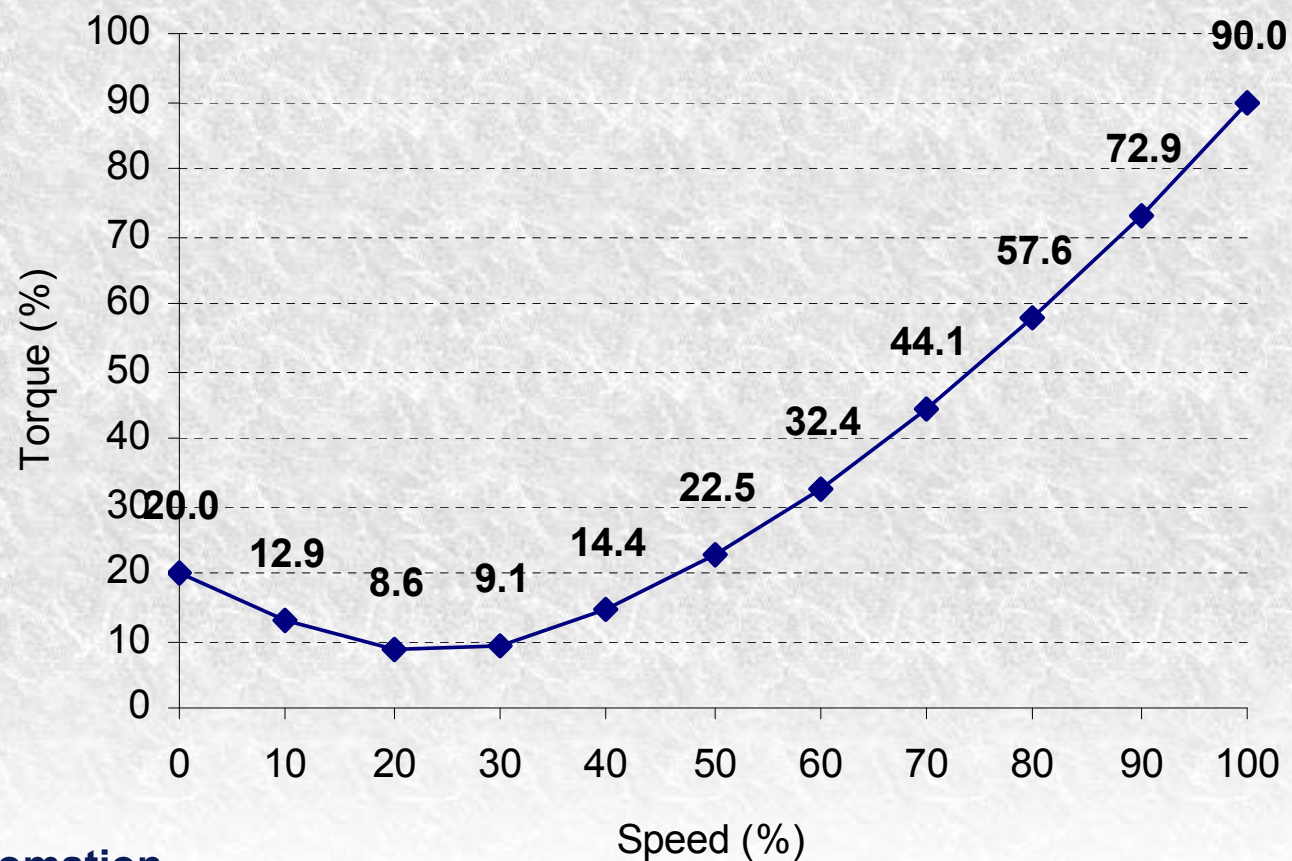


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Calculation example 计算举例

- A fan has following load characteristics

一个风机有如下的负载特性



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Calculation example 计算举例

- ➔ A following motor has been selected:

电机选型如下

$$P_n = 110 \text{ kW}$$

$$U_n = 400 \text{ V}$$

$$I_n = 202 \text{ A}$$

$$\cos(\phi_n) = 0.83$$

$$n_n = 991 \text{ rpm}$$

$$J_{\text{motor}} = 5 \text{ kgm}^2$$

- ➔ Fans moment of inertia is $J_{\text{fan}} = 995 \text{ kgm}^2$

风机转动惯量: $J_{\text{fan}} = 995 \text{ kgm}^2$

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Calculation example 计算举例

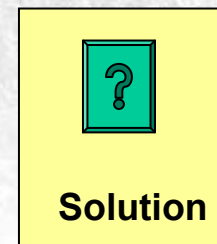
- **Task 1: What is the nominal torque of the motor? What is the nominal efficiency of the motor?**

电机的额定力矩是多少？

电机的额定效率是多少？

- **Task 2: Estimate the starting time from 0 to 100% speed if accelerating is done with nominal torque.**

如果以额定力矩加速，估算电机转速从0上升到100%的额定速度的起动时间。



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Calculation example

Task 3: Estimate the deceleration time from 100% to 0% speed if it is assumed that the average braking torque over the whole speed range (in generating mode, flux braking is utilised) is 4.5%.

***Hint:* Divide the speed range into sectors and calculate the times over the sectors.**

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Calculation example - Solution

Task 1:

➤ Nominal torque of the motor is: 电机的额定力矩

$$T_n [Nm] = \frac{9550 * P_n [kW]}{n_n [rpm]} = \frac{9550 * 110}{991} Nm \approx 1060 Nm$$

➤ Nominal efficiency of the motor is: 电机的额定效率

$$\eta_n = \frac{P_{out}}{P_{in}} = \frac{P_n [W]}{\sqrt{3} * U_n [V] * I_n [A] * \cos(\varphi_n)} = \frac{110000}{\sqrt{3} * 400 * 202 * 0.83} \approx 0.947$$

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Calculation example - Solution

Task 2:

- Speed range is divided into 10 sectors. 速度范围分成10段
- Acceleration time for each sector is calculated using formula:

每一段的加速时间用下列公式计算

$$\Delta t[s] = J[kgm^2] * \frac{2\pi}{60} * \frac{\Delta n[rpm]}{T_{dyn}} = J[kgm^2] * \frac{2\pi}{60} * \frac{\Delta n[rpm]}{T_n - T_{load}}$$

- In each sector average value of load torque is used. For example in sector 1 the average load torque is $(20+12.9)/2 \% = 16.45 \%$ and the dynamic accelerating torque $(T_n - T_{load})$ is $100 \% - 16.45 \% = 83.55 \%$.

每段都使用负载力矩的平均值。例如第一部分的平均力矩是：

$(20+12.9)/2 \% = 16.45 \%$,

动态加速力矩 $(T_n - T_{load})$ 是：

$100 \% - 16.45 \% = 83.55 \%$.

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Calculation example - Solution

Task 2:

$$0 - 99.1 \text{ rpm} \quad \Delta t[s] = J[\text{kgm}^2] * \frac{2\pi}{60} * \frac{\Delta n[\text{rpm}]}{T_n - T_{load}} = 1000 * \frac{2\pi}{60} * \frac{99.1}{0.8355 * 1060} \text{ s} = 11.7 \text{ s}$$

$$99.1 - 198.2 \text{ rpm} \quad \Delta t[s] = 1000 * \frac{2\pi}{60} * \frac{99.1}{0.8925 * 1060} \text{ s} = 11.0 \text{ s}$$

$$198.2 - 297.3 \text{ rpm} \quad \Delta t[s] = 1000 * \frac{2\pi}{60} * \frac{99.1}{0.9115 * 1060} \text{ s} = 10.7 \text{ s}$$

$$297.3 - 396.4 \text{ rpm} \quad \Delta t[s] = 1000 * \frac{2\pi}{60} * \frac{99.1}{0.8825 * 1060} \text{ s} = 11.1 \text{ s}$$

$$396.4 - 495.5 \text{ rpm} \quad \Delta t[s] = 1000 * \frac{2\pi}{60} * \frac{99.1}{0.8155 * 1060} \text{ s} = 12.0 \text{ s}$$

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Calculation example - Solution

Task 2:

$$495.5 - 594.6 \text{ rpm} \quad \Delta t[s] = 1000 * \frac{2\pi}{60} * \frac{99.1}{0.7255 * 1060} s = 13.5 s$$

$$594.6 - 693.7 \text{ rpm} \quad \Delta t[s] = 1000 * \frac{2\pi}{60} * \frac{99.1}{0.6175 * 1060} s = 15.9 s$$

$$693.7 - 792.8 \text{ rpm} \quad \Delta t[s] = 1000 * \frac{2\pi}{60} * \frac{99.1}{0.4915 * 1060} s = 19.9 s$$

$$792.8 - 891.9 \text{ rpm} \quad \Delta t[s] = 1000 * \frac{2\pi}{60} * \frac{99.1}{0.3475 * 1060} s = 28.2 s$$

$$891.9 - 991 \text{ rpm} \quad \Delta t[s] = 1000 * \frac{2\pi}{60} * \frac{99.1}{0.1855 * 1060} s = 52.8 s$$

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Calculation example - Solution

Task 2:

- ➔ The total acceleration time is the sum of all sector times: 186.8 seconds! 总时间为每段时间之和
- ➔ Sector width affects the accuracy of this kind of approximation. 每一部分的宽度影响近似类型的精度

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Calculation example - Solution

Task 3:

- ➔ Speed range is divided into 10 sectors.
- ➔ Deceleration time for each sector is calculated using formula ($T = -4.5\%$):

$$\Delta t[s] = J[kgm^2] * \frac{2\pi}{60} * \frac{\Delta n[rpm]}{T_{dyn}} = J[kgm^2] * \frac{2\pi}{60} * \frac{\Delta n[rpm]}{T_{load} + T}$$

- ➔ In each sector average value of load torque is used. For example in sector 10 the average load torque is $(90+72.9)/2 \% = 81.45 \%$ and the dynamic decelerating torque is $81.45\% + 4.5 \% = 85.95 \%$.

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Calculation example - Solution

Task 3:

$$991 - 891.9 \text{ rpm} \quad \Delta t[s] = 1000 * \frac{2\pi}{60} * \frac{99.1}{0.8595 * 1060} s = 11.4 s$$

$$891.9 - 792.8 \text{ rpm} \quad \Delta t[s] = 1000 * \frac{2\pi}{60} * \frac{99.1}{0.6975 * 1060} s = 14.0 s$$

$$792.8 - 693.7 \text{ rpm} \quad \Delta t[s] = 1000 * \frac{2\pi}{60} * \frac{99.1}{0.5535 * 1060} s = 17.7 s$$

$$693.7 - 594.6 \text{ rpm} \quad \Delta t[s] = 1000 * \frac{2\pi}{60} * \frac{99.1}{0.4275 * 1060} s = 22.9 s$$

$$594.6 - 495.5 \text{ rpm} \quad \Delta t[s] = 1000 * \frac{2\pi}{60} * \frac{99.1}{0.3195 * 1060} s = 30.6 s$$

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Calculation example - Solution

Task 3:

$$495.5 - 396.4 \text{ rpm} \quad \Delta t[s] = 1000 * \frac{2\pi}{60} * \frac{99.1}{0.2295 * 1060} s = 42.7 s$$

$$396.4 - 297.3 \text{ rpm} \quad \Delta t[s] = 1000 * \frac{2\pi}{60} * \frac{99.1}{0.1625 * 1060} s = 60.2 s$$

$$297.3 - 198.2 \text{ rpm} \quad \Delta t[s] = 1000 * \frac{2\pi}{60} * \frac{99.1}{0.1335 * 1060} s = 73.3 s$$

$$198.2 - 99.1 \text{ rpm} \quad \Delta t[s] = 1000 * \frac{2\pi}{60} * \frac{99.1}{0.1525 * 1060} s = 64.2 s$$

$$99.1 - 0 \text{ rpm} \quad \Delta t[s] = 1000 * \frac{2\pi}{60} * \frac{99.1}{0.2095 * 1060} s = 46.7 s$$

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Calculation example - Solution

Task 3:

- ➔ The total deceleration time is the sum of all sector times: 383.7 seconds!
- ➔ Sector width affects the accuracy of this kind of approximation.